Digital Image Processing

Morphological Image Processing (2)

Color Representation

Topics

- Morphological Operations
 - Connected Component Extraction
 - Convex Hull
 - Thinning
 - Thickening
 - Skeleton
 - Pruning
 - Extension to gray level images
 - Matlab Examples

Dilation and Erosion

- Dilation and Erosion are two basic operations in morphological processing.
- Dilation of a set A in Z^2 by a set B in Z^2 is denoted by A \bigoplus B and given by

$$A \oplus B = \{ z | (\hat{B})_z \cap A \neq \emptyset \}$$

Dilation

- The dilation of A by B is the set of all displacements such that A and \hat{B} overlap with at least one point
- B is called structuring element

Dilation



Erosion

Erosion of a set A in Z² by a set B in Z² is denoted by
 A ⊖ B and given by:

$A \ominus B = \{ z | (B)_z \subseteq A \}$

Erosion of A by B is the set of all points z such that B translated by z is contained in A



Opening

- Opening smoothes the outer contours, breaks narrow connections, and eliminates small protrusions.
- Opening is defined as :

 $A \circ B = (A \ominus B) \oplus B$

Closing

• Closing smoothes the object contour, fuses narrow connections, eliminates small holes and gaps.

 $A \bullet B = (A \oplus B) \ominus B$

Extraction of Connected Components

• Begin with a point P inside the connected component, iterate:

$$X_k = (X_{k-1} \oplus B) \cap A \quad k = 1, 2, 3, \dots$$

Until $X_k = X_{k-1}$ Initially $X_0 = P$

Connected Component Extraction







Convex Hull

- A set is said convex if the straight line connecting any two points of the set lies entirely within A.
- Convex Hull of set S is the smallest convex set A that contains S
- The set difference A-S is called the convex deficiency of S

Computing Convex Hull

• Let B_i for i=1,2,3,4 represent the structuring elements shown below



Convex Hull

• Repeat the following equation until converge

 $X_k^i = (X_{k-1} \circledast B^i) \cup A \quad i = 1, 2, 3, 4 \text{ and } k = 1, 2, 3, \dots$ with

 $X_0^i = A$ (*) is the Hit-or-Miss operator

Assuming
$$D^i = X^i_{\text{conv}}$$
 Convex Hull is $C(A) = \bigcup_{i=1}^4 D^i$

Example (Convex Hull)



Improving Convex Hull Algorithm

• The algorithm can be improved by limiting the growth of the algorithm beyond the maximum dimensions of the original set.



Thinning and Thickening

- Thinning is an image-processing operation in which binary valued image regions are reduced to lines
- The purpose of thinning is to reduce the image components to their essential information for further analysis and recognition
- Thickening is changing a pixel from 1 to 0 if any neighbors of the pixel are 1.
- Thickening followed by thinning can be used for filling undesirable holes.
- Thinning followed by thickening is used for determining isolated components and clusters.

Thinning

• Thinning is defined in terms of hit or miss as

$$A \otimes B = A - (A \circledast B)$$
$$= A \cap (A \circledast B)^{c}.$$

where B is a sequence of structuring elements like $\{B\} = \{B^1, B^2, B^3, \dots, B^n\}$ and the operation can be given as

$$A \otimes \{B\} = \left(\left(\dots \left(\left(A \otimes B^1 \right) \otimes B^2 \right) \dots \right) \otimes B^n \right)$$

Thinning

• Sample set of structuring elements



Thinning Example

- Origin





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1	NA.	D.
A	S S	n







		200		5		

4	0	D7.8
A	S	B',0

 $A \otimes B^{1,2,3}$

Thickening

• Thickening is the morphological dual of thinning and defined as

or
$$A \odot B = A \cup (A \circledast B)$$

 $A \odot \{B\} = \left(\left(\ldots \left(\left(A \odot B^1 \right) \odot B^2 \right) \ldots \right) \odot B^n \right) \right)$

Thickening Example



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Skeleton

- The informal definition of a skeleton is a line representation of an object that is:
 - one-pixel thick,
 - through the "middle" of the object, and,
 - preserves the topology of the object.



Skeleton

• Skeleton is defined by

$$S(A) = \bigcup_{k=0}^{K} S_k(A)$$

where

$$S_k(A) = (A \ominus kB) - (A \ominus kB) \circ B$$

k is the last iterative step before A erodes to an empty set

$$K = \max\{k \mid (A \ominus kB) \neq \emptyset\}$$

Skeleton Example



Pruning

- Thinning and skeletonizing algorithms need a clean-up postprocessing
- The following steps are used for pruning:
 - Thinning $X_1 = A \otimes \{B\}$
 - Find the end points

• Dilate end points

$$X_2 = \bigcup_{k=1}^8 (X_1 \circledast B^k)$$

 $X_3 = (X_2 \oplus H) \cap A$

• Find the union of X1 and X3

$$X_4 = X_1 \cup X_3$$

Pruning Example

• Original image and structuring elements



Pruning Example

• Result of thinning and end points detected



Pruning Example

• Dilation of end points and the pruned image



Extension to Gray Level

• Dilation is expressed in 1D as

$$(f \oplus b)(s) = \max\{f(s-x) + b(x) | (s-x) \in D_f \text{ and } x \in D_b\}$$

• Erosion is given by

 $(f \ominus b)(s) = \min\{f(s + x) - b(x) | (s + x) \in D_f \text{ and } x \in D_b\}$

Extension to Gray Level (2D Case)

• Dilation

 $(f \oplus b)(s, t) = \max\{f(s - x, t - y) + b(x, y) | (s - x), (t - y) \in D_f; (x, y) \in D_b\}$

• Erosion

 $(f \ominus b)(s, t) = \min\{f(s + x, t + y) - b(x, y) | (s + x), (t + y) \in D_f; (x, y) \in D_b\}$

Morphological Operations in MATLAB

• To create structuring element use strel(.)

SE = strel(*shape*, parameters)

Examples:

$$SE = strel('diamond', R)$$

$$SE = strel('disk', R, N)$$

$$SE = strel('line', LEN, DEG)$$

$$SE = strel('octagon', R)$$

Morphological Operations in MATLAB

- SE=strel(NHOOD) is also a valid call for the function
- Use imerode(Im,SE) and imdialte(Im,SE) for erosion and dilation respectively
- Use imopen(Im,SE) and imcolose(Im,SE) for openning and closing
- For hit-or-miss use bwhitmiss(.)
 - BW2 = bwhitmiss(BW1,SE1,SE2)
 BW2 = bwhitmiss(BW1,INTERVAL)

Hit or Miss Example

 $bw = \begin{bmatrix} 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 1 & 0 & 0 \\ 0 & 1 & 1 & 1 & 1 & 0 \\ 0 & 1 & 1 & 1 & 1 & 0 \\ 0 & 0 & 1 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \end{bmatrix}$

interval = [0 -1 -1 1 1 -1 0 1 0];

bw2 = bwhitmiss(bw,interval)

bw2 =

0	0	0	0	0	0
0	0	0	1	0	0
0	0	0	0	1	0
0	0	0	0	0	0
0	0	0	0	0	0
0	0	0	0	0	0

Color Representation

Color Representation: Motivation

- Color is an important feature for detecting and identifying objects
 - Human face detection
 - License plate detection
 - Content based image retrieval systems
- Image segmentation can be performed base on color values
- Tracking moving objects in video (surveillance)
- Etc.

Color Spectrum





Visible Wavelength

Absorption of light by human eye



Red, Green, Blue Color Cube



RGB Color Cube



YIQ Color Model

- YIQ is the color space used by the NTSC color TV system
- The Y component represents the luma information, and is the only component used by black-and-white television receivers
- I and Q represent the chrominance information
- For example, applying a histogram equalization to a color image is done by Y component only

YIQ Color Model Conversion

$$\begin{bmatrix} R \\ G \\ B \end{bmatrix} = \begin{bmatrix} 1 & 0.9563 & 0.6210 \\ 1 & -0.2721 & -0.6474 \\ 1 & -1.1070 & +1.7046 \end{bmatrix} \begin{bmatrix} Y \\ I \\ Q \end{bmatrix}$$

[Y]		0.299	0.587	0.114	$\lceil R \rceil$
I	=	0.595716	-0.274453	-0.321263	G
$\lfloor Q \rfloor$		0.211456	-0.522591	0.311135	$\lfloor B \rfloor$



Conversion from RGB to HSI

$$H = \begin{cases} \theta & \text{if } B \leq G \\ 360 - \theta & \text{if } B > G \end{cases}$$

with $\theta = \cos^{-1} \left\{ \frac{\frac{1}{2} [(R - G) + (R - B)]}{[(R - G)^2 + (R - B)(G - B)]^{1/2}} \right\}$ $S = 1 - \frac{3}{(R + G + B)} [\min(R, G, B)]$ $I = \frac{1}{3} (R + G + B)$

Enhancement using HSI Model



Color Space Conversions in MATLAB (1)

- To convert from RGB to HSV use rgb2hsv
- For HSV to RGB conversion use hsv2rgb
- E.g.
 - I = imread('test.bmp');
 - H = rgb2hsv(I);



Color Space Conversions in MATLAB (2)

- To convert from RGB color space into YIQ color space use rgb2ntsc
 - RGB = imread('sample.png');
 - YIQ = rgb2ntsc(RGB);
- ntsc2rgb convert from YIQ to RGB
- Images can be displayed in RGB space only

Color Space Conversions in MATLAB (3)

- I component in YIQ (the first component) is equivalent to a gray scale conversion. However, you may also use rgb2gray either.
 - I=imread('test.bmp');
 - YIQ = rgb2ntsc(I);
 - imshow(YIQ(:,:,1))



Questions?